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## IncClase Uorefoook

## The Number System:

Unit 2: Multiplying \& Dividing Rational Numbers

## How can we classify different numbers, describe what they represent and their relationship with each other?

| Standard | Description |
| :--- | :--- |
| 7.NS.A.2 | Apply and extend previous understandings of multiplication and division and of fractions to multiply <br> and divide rational numbers. <br> a: Understand that multiplication is extended from fractions to rational numbers by requiring that <br> operations continue to satisfy the properties of operations. <br> b: Understand that integers can be divided, provided that the divisor is not zero, and every quotient <br> of integers (with non-zero divisor) is a rational number. <br> c: Apply properties of operations as strategies to multiply and divide rational numbers. |
| 7.NS.A.3 | Solve real-world and mathematical problems involving the four operations with rational numbers. |


| Packet Completion Rubric |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{1}$ | o |  |
| Workbook demonstrates <br> significant effort. Student <br> utilizes notes to help <br> extend their thinking, <br> writing questions, <br> comments or reactions to <br> the content. | Workbook <br> demonstrates some <br> effort. Student takes <br> notes but could <br> further understanding <br> by questioning and <br> interacting with the <br> material. | Workbook shows little <br> effort. Student takes <br> notes sporadically, and <br> could benefit from <br> greater consistency with <br> the material. | Workbook shows little <br> to no effort. Student <br> does not take notes and <br> must demonstrate <br> future interaction with <br> the material to aid <br> understanding. | Workbook is entirely <br> incomplete or not <br> turned in. |  |

Grading Breakdown: 3.5-4 = A 3-3.4 = B 2.5-2.9 = C 2-2.4 = D $\quad$ 0-1.9 $=$ F
I am a person who believes in asking questions, in not conforming for the sake of conforming. I am deeply dissatisfied - about so many things, about injustice, about the way the world works - and in some ways, my dissatisfaction drives my storytelling.

Chimamanda Ngozi Adichie

Add to the mind map below as you develop your understanding of the guiding question.

## Unit 2 Guiding Questions:

How is a product or quotient positive, negative, or zero? Why?
How can diagrams and models be used to visualize multiplication and division with rational numbers?

| Lesson Objectives |  |
| :---: | :--- |
| Lesson <br> After completing a <br> lesson, check the box | I can... $\quad$ After completing each lesson, you are on the right track if you can confidently state "I can..." |
| $\square$ | Multiply rational numbers. |
| $\square$ | Divide rational numbers. |
| $\square$ | Interpret products and quotients of rational numbers by describing real -world contexts. <br> $\square$ |
|  | Solve and justify my answer when adding, subtracting multiplying and dividing rational <br> numbers. |


| DO-NOW | 1. Hannah made strawberry jam and raspberry jam. She made enough strawberry jam to fill $1 / 2$ of a jar. If she made 4 times as much raspberry jam as strawberry jam, how many jars will the raspberry jam fill? <br> 2. Addie bought 9 candy bars and ate $1 / 3$ of them, Fran bought 6 candy bars and ate $2 / 3$ of them. Who ate more candy bars? |
| :---: | :---: |
| Homework Reminder | This is where you will shade in the box if you turned in your homework. There is no homework due today! :) <br> "We become what we repeatedly do."-Sam Covey |
| Check-In | How are you doing today? <br> What do you remember from learning how to multiply fractions from last year? |

What strategies can we use to multiply fractions?
What are the two parts of a fraction?
Fractions show a part to whole relationship.
Fractions can also show division: $\qquad$

Yesenia wants to know the area of her vegetable garden. What is the area of her garden if it is $1 \frac{1}{3}$ yards by $1 \frac{1}{2}$ yards?

What is the popcorn method?


How do we simplify fractions?

Practice Problems

1. $\frac{1}{3} \times \frac{2}{4}$
2. $5 \frac{1}{4} \times 2 \frac{1}{6}$
3.) $2.4 \times 6.8=$ $\qquad$ 4.) $3.56 \times 8.9=$ $\qquad$

Rational Numbers Recap: What does this diagram mean?


A rational number is any number that can be $\qquad$ as a $\qquad$ (fraction). $\frac{1}{3}=$ $\qquad$ . This is an example of a $\qquad$ -
$\frac{1}{4}$ $4=$ $\qquad$ . This is an example of a $\qquad$ .

In Summary: Rational numbers always $\qquad$ or $\qquad$ as decimals.

You Try! Use long division to determine whether or not these fractions are repeating or terminating decimals. Circle your answer! DO NOT USE A CALCULATOR!

1. $\frac{2}{11}$
2. $\frac{5}{8}$
3. $\frac{7}{9}$

Repeating or Terminating? Repeating or Terminating? Repeating or Terminating?

## EXPLORING MULTIPLICATION ADD RATIONAL NUMBERS

You and your partner are going to have a set of red and yellow tokens. The red side is negative and the yellow side is positive. Together, you will need to solve problems using the tokens to help you represent the values of the numbers. Do your best and be sure to explain your final answer - you need to justify why you think it is correct! If you are stuck, think about what information would help you solve the problem. Feel free to draw a picture to represent your tokens.

| Problem 1: $\quad 2 \times 4=$ |
| :--- |
| Explain and Justify: |

Problem 2: $-3 \times 4=$ $\qquad$
Explain and Justify:

Problem 3: $\quad-1$ * 8 = $\qquad$ Explain and Justify:
$\qquad$

Problem 4: $\quad-2 \times-4=$ $\qquad$
Explain and Justify:
$\qquad$
$\qquad$

Problem 5:
$-1 \cdot-3=$ $\qquad$
Explain and Justify:

## Exploration Recap

What is similar about how these were solved to what you did?

What is different about how these were solved to what you did?

What language (words) are used during this process?

## What do you notice about the sign of the numbers that you are multiplying and the sign of the product?

Rules for Multiplying Positive and Negative Numbers Positive $\times$ Positive =

Positive $\times$ Negative $=$

Negative x Negative =

Mini Practice

$$
\begin{array}{llll}
3^{*-6}= & -8 \times-2= & -7^{*} 0= & (-1)(5)= \\
4 \times-5= & -10(4)= & 16^{*}-2= & 12^{*} 1^{*}-3=
\end{array}
$$

## Summary and Recap



## Sleepy Man

Same signs answer is $\qquad$ .

Different signs answer is $\qquad$ .

| Rules for Multiplying AND Dividing |  |  |
| :---: | :---: | :---: |
| Sign of 1st Number | Sign of 2nd Number | Sign of Answer |
| + | + |  |
| + | - |  |
| - | + |  |
| - | - |  |

## Practice, Practice Practice

Team Member Name 1: $\qquad$
Their favorite color: $\qquad$

Team Member Name 2: $\qquad$
Their favorite color: $\qquad$

Team Member Name 3: $\qquad$
Their favorite color: $\qquad$

Team Member Name 4: $\qquad$
Their favorite color: $\qquad$
Solve the problems on the following page. Show ALL of your work and justify your answer.

## Multiplying Integers

1. $(-8) \times 7=$
2. $1 \times 5=$ $\qquad$
3. $(-11) \times(-6)=$ $\qquad$ 4. $(-3) \times(-4)=$ $\qquad$
4. $(-9) \times 13=$ $\qquad$ 6. $-12 \times(0)=$ $\qquad$

## Multiplying Decimals

7. $0.002 \times 0.005=$ $\qquad$
8. $0.011 *(-0.1)=$ $\qquad$
9. 0.09 * $-1.1=$ $\qquad$

## Multiplying Fractions

13. $-\frac{3}{6} \cdot \frac{2}{3}=$ $\qquad$
14. $-\frac{4}{6} \times\left(-\frac{9}{10}\right)=$ $\qquad$
15. $-\frac{10}{12} \cdot\left(\frac{2}{5}\right)=$ $\qquad$
16. $\frac{2}{4} \cdot \frac{11}{4}=$ $\qquad$
Multiplying Mixed Numbers
17. $-1 \frac{4}{9} \cdot 4 \frac{1}{4}=$ $\qquad$
18. $-2 \frac{7}{10} \times\left(-\frac{9}{10}\right)=$ $\qquad$
19. $-\frac{10}{12} \cdot\left(1 \frac{3}{4}\right)=$ $\qquad$
20. $-1 \frac{2}{3} \cdot-2 \frac{5}{6}=$ $\qquad$

|  | collected $21 / 4$ times as much clothing as Nate's class. How many pounds of clothing did Tony's <br> class collect? |
| :--- | :---: |
| 2. $\quad$Zach collected 8 pounds of newspaper for the recycling drive. Alexa collected $31 /$ times as <br> much newspaper as Zach. How many pounds of newspaper did Alexa collect? <br> Homework <br> Reminder <br> Check-In <br> How are you doing today? <br> "We become what we repeatedly do." - Sam Covey |  |

Is the quotient of two integers always an integer?

Think Space:

Examples:

- Consider the following:
- However, consider:

Conclusion:

## Rules for Dividing Positive and Negative Numbers

 Positive $\div$ Positive $=$- Ex: $\qquad$
Positive $\div$ Negative $\underline{\text { OR Negative }} \div$ Positive $=$
- Ex: $\qquad$
Negative $\div$ Negative $=$
- Ex: $\qquad$


## Same or Different?

1. $-14 \div 7=$
2. $14 \div(-7)=$
3. $-(14 \div 7)=$

Are the answers to these problems the same or different? Why?

## Dividing with Rational Numbers

How to Divide Fractions: Keep - Change - Flip!
$\qquad$

Let's try it out!

$$
\frac{4}{7} \div \frac{7}{2}=?
$$

$$
\frac{3}{5} \div \frac{1}{9}=?
$$

$$
\frac{4}{3} \div \frac{7}{8}=?
$$

How do I divide decimals?!

## Scoot those decimals over!

Find the quotient.


Video Notes

Let's Get Some Practice: Take two cards and make a fraction!

1. Fill in your partner's name in the chart below.
2. With your partner, you will each pick two cards from the deck at your table each round. The first card will be the numerator, the second card is the denominator. $(J=11, Q=12, K=13$, Ace = 1)
Red $=$ Negative
Black $=$ Positive
3. Working with your partner, divide fractions (the partner who is oldest will place
 the dividend). Divide and show all of your work.
4. Once you have solved the problem, compare answers with your partner. If it's correct, write the answer in the final column labelled, "Quotient."

| Rounds | Dividend | Divisor | Quotient |
| :---: | :---: | :---: | :---: |
| 1 |  |  |  |
| 2 |  |  |  |
| 3 |  |  |  |
| 4 |  |  |  |
| 5 |  |  |  |
| 6 |  |  |  |
| 8 |  |  |  |

## Show your work here:

| 1. | 2. | 3. | 4. |
| :--- | :--- | :--- | :--- | :--- |
| 5. | 6. | 7. | 8. |
|  |  |  |  |


| DO-NOW | 1. Find a reason why each number doesn't belong. <br> 2. Find the mistake in this person's work and explain what they should do differently. <br> Problem: $3 / 4 \div 5 / 6$ <br> Step 1: <br> 3/4* \% <br> Step 2: |
| :---: | :---: |
| Homework Reminder | Shade in this box if you turned in your homework. <br> "We become what we repeatedly do."-Sam Covey |
| Check-In | How are you doing today? <br> What mathematical ideas are you wondering about today? What problems are you trying to solve? |


| Strategies for Solving Word Problems |
| :--- |
| SOLVINGSTEPS |
| $\square$ STEP I: UNDERSTAND THE PROBLEM. |
| $\square$ STEP 2: MARE A PLAN. |
| $\square$ STEP S: SOLVE IT. |
| $\square$ STEP 4: CHECK IT. |
| $\rightarrow$ Box the main question(s). |

$\rightarrow$ Underline only the parts needed to answer the question(s).
$\rightarrow$ Circle vocabulary, keywords, and important units.
$\rightarrow$ Knock out irrelevant information.
$\rightarrow$ Solve \& CHECK!
Video Tutorial: As you watch the following video, annotate the word problems using the BUCKS strategy and solve the problem in the space provided.

At a shop on Times Square, three "I $\quad$ NY" t-shirts sell every 10 minutes for $\$ 19.95$ each. Every 45 minutes one Yankees hat sells for $\$ 24.95$. The shop is open from 9am to 9 pm every day. How many t-shirts are sold in a week?

Larkin's family had a garage sale. Her parents said that she could sell some of her old toys. Larkin decided to sell all of her stuffed animals. She sold 7 big stuffed animals for $\$ 2.50$ each and 13 small ones for $\$ 0.75$ each. Larkin took some of the money she made to a garage sale down the street. There were a lot of books at that sale. Hardbacks were $\$ 0.50$ and paperbacks were just $\$ 0.25$. Larkin spent $\$ 5.75$ for 17 books. She also bought a game for $\$ 1.50$ and 18 pretty marbles for a nickel each. She gave the marbles to her little sister, then they played the new game until dinnertime. How much money did Larkin have left?

## Adding and Subtracting Fractions \& Mixed Numbers Task Cards

Record your answers to each task card here. Show ALL of your work in each box and explain your answer. CIRCLE your final answer!

| Task Card \# 1 | Task Card \# 2 |
| :--- | :--- |
|  |  |
| Task Card \# 3 |  |
| Task Card \# 5 | Task Card \# 4 |
| Task Card \# 7 |  |


| DO-NOW | 1. $-54,432 \div-12$ | 2. $-48 \div(-4) \div(-4)$ |
| :--- | :---: | :---: |
| Homework <br> Reminder | Shade in this box if you turned in your homework. <br> "We become what we repeatedly do." - Sam Covey |  |
| Check-In | How are you doing today? |  |
| What has been your favorite math lesson this year? |  |  |

## Questions and Discussion

| 1. How do we determine if the product of two signed <br> numbers will be positive or negative? | 2. Why does the product of two negative values result in a <br> positive value? |
| :--- | :--- |
| Thoughts: | Thoughts: |
| Final thought: | Final thought: |
| Evidence: | Evidence: |

## Solve with a Partner

Kathleen collected $1 / 4$ of a bin of glass bottles to recycle. Garrett collected $73 / 5$ times as many bins as Kathleen. How many bins of bottles did Garrett collect?

Solve:

Justify and Explain:

## Mixed Practice

## Section 1: Evaluate each expression and circle/highlight your final answer.

1. $(-7)+(-4)+7$
2. $(-4)+8-(-2)$
3. $(-1)-(-4)-(-3)$
4. $(-1)-4+6$

Choose one problem from the set above and EXPLAIN IN DETAIL how you solved it. Feel free to use words and pictures to explain it.

Section 2: Find each product and circle/highlight your final answer. Remember: write your answer in simplest form!

1. $7 \cdot-6 \cdot 6$
2. $-10 \cdot-9 \cdot-1$
3. $-7 \cdot 6 \cdot-8$
4. $-3 \cdot 2 \cdot-6$
5. $-\frac{5}{3} \cdot-\frac{3}{4}$
6. $-\frac{7}{4} \cdot 3 \frac{1}{2}$

Choose one problem from the set above and EXPLAIN IN DETAIL how you solved it. Feel free to use words and pictures to explain it.

Section 3: Find each quotient and circle/highlight your final answer..Remember: write your answer in simplest form!

1. $7 \div-1$
2. $6 \div 3$
3. $-6 \div 6$
4. $-45 \div 9$
5. $-\frac{3}{4} \div \frac{5}{8}$
6. $-2 \frac{1}{5} \div-\frac{-6}{5}$

Choose one problem from the set above and EXPLAIN IN DETAIL how you solved it. Feel free to use words and pictures to explain it.

Section 4: Evaluate each expression and circle/highlight your final answer. Remember: write your answer in simplest form!

1. $(-6.3)-(-7.46)$
2. $(-3.4)-1.5$
3. $\frac{8}{5}-\left(-\frac{4}{5}\right)$
4. $\left(-1 \frac{1}{2}\right)+\frac{3}{4}$
5. $(-30-10) \div-4+-5-2$
6. $5 \cdot 8+2-(-6--5)$

Choose one problem from the set above and EXPLAIN IN DETAIL how you solved it. Feel free to use words and pictures to explain it.

Section 5: Solve the following word problems. Remember: write your answer in simplest form!

1. Aidan, a pet store employee, wants to fit two fish tanks on one table. One fish tank is $25 / 6$ feet wide and the other fish tank is $2 / 3$ of a foot wide. When placed next to each other, what is the total width of the two fish tanks?
2. Ava sprinted $5 / 8$ of a lap and then took a break by jogging $3 / 8$ of a lap. How much farther did Ava sprint than jog?
3. On Monday a team of beach volunteers cleaned $43 / 5$ beaches. Tuesday, the team cleaned $11 / 2$ times as many beaches as on Monday. How many beaches did the beach volunteers clean on Tuesday?
4. Bella made $1 / 2$ of a quart of POG. Each mug holds $1 / 10$ of a quart. How many mugs will Bella be able to fill?

Choose one problem from the set above and EXPLAIN IN DETAIL how you solved it. Feel free to use words and pictures to explain it.

## compare and share

| Name: <br> Summary: | Name: <br> Summary: |
| :--- | :--- |
| Name: <br> Summary: | Name: <br> Summary: |

## Workbook Reflection

Answer the question as completely as possible, using evidence from what we have learned this unit. Justify your response with examples and evidence from throughout the packet.

Choose one of the following questions to answer using words or pictures: Is the product or quotient positive, negative, or zero? Why? How can multiplying and dividing rational numbers help us make real life decisions? How can number lines and diagrams be used to visualize mathematical operations with rational numbers?

Evaluate your understanding of multiplying and dividing rational numbers on a scale from 0-4 and explain why you feel that way:

## What lesson most challenged your thinking?

What was your favorite/least favorite lesson and why?

Flip through your packet, and look to see if you shaded the box every day for turning in your homework. How many days did you shade it in?

| Lesson 1 | Lesson 2 | Lesson 3 | Lesson 4 |
| :--- | :--- | :--- | :--- |

If you didn't finish it each night, consider why $\rightarrow$

Would you like to come in during lunch or recess for support?

